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## Analysis of the Dependence between Acoustic and Physico-Mechanical **Properties of Terrigenic Rocks**

# Dmitrii G. Petrakov, Grigorii M. Penkov, Dmitry A. Solomoychenko

Saint Petersburg Mining University (2 21st line, Vasilyevsky island, Saint Petersburg, 199106, Russian Federation)

Анализ зависимости между акустическими и физико-механическими свойствами горных пород терригенных отложений

## Д.Г. Петраков, Г.М. Пеньков, Д.А. Соломойченко

Санкт-Петербургский горный университет (Россия, 199106, г. Санкт-Петербург, Васильевский остров, 21-я линия, 2)

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During the entire development of the oil and gas field, it is necessary to carry out a complex of various studies aimed at identifying the parameters of the productive layer. One of such studies is the analysis of core material, as a result of which the following parameters of the rock are determined: porosity, permeability, Young's modulus and others. The listed characteristics must be taken into account when building a geological and hydrodynamic model of a field. In addition to these parameters, the strength properties of the rock should be determined, since they are necessary in the design of the wellbore. Such characteristics Keywords: Young's modulus, longitudinal wave, transverse wave, ultimate strength in volumetric compression, effective stress, acoustic properties. can be obtained by conducting research in specialized laboratories. This is not always possible due to various reasons. A number of studies confirm the fact of the relationship between the acoustic properties of a rock (the velocity of the longitudinal and transverse waves) and the strength characteristics. The acoustic properties of the rock must be taken into account when interpreting the acoustic logs of the wells, which allows to reveal the distribution of rocks along the wellbore. Based on the velocities of ultrasonic waves propagation, it is possible to calculate the dynamic modulus of elasticity, which allows to assess the tendency of the rock skeleton to compaction as a result of the effective stress action. Therefore, determination of the rock acoustic properties is necessary when planning the field development and its implementation. The results of laboratory studies aimed at establishing the relationship between the strength and acoustic properties of rocks are presented. During the experiment, the dynamic Young's modulus was also determined and its relationship with the speed of ultrasonic waves propagation was revealed. As a result of laboratory studies, empirical dependences of the ultimate strength in volumetric compression ( $\sigma_{\rho}$ ), dynamic modulus of elasticity (*E*) and the velocity of transmission of longitudinal ( $v_{\rho}$ ) and transverse ( $v_{\rho}$ ) waves were obtained. An assessment of the obtained values was given over the entire measurement range. Ключевые слова: Во время всей разработки нефтяного и газового месторождения необходимо проводить комплекс различных исследований, направленных на выявление параметров продуктивного горизонта. Одним из таких исследований является анализ кернового материала, в результате которого определяются следующие параметры горной породы: пористость, модуль Юнга, продольная волна, поперечная волна, предел произдемость, модуль Юнга и другие. Перечисленные характеристики необходимо учитывать при построении геологической и гидродинамической модели месторождения. Помимо этих параметров следует определять прочностные свойства горной породы, так как они необходимы при проектировании ствола скважины. Такие характеристики можно прочности при объемном сжатии, эффективное напряжение, акустические свойства. получить, проведя исследования в специализированных лабораториях. Это не всегда возможно вследствие различных причин. Ряд исследований подтверждает факт зависимости между акустическими свойствами горной породы (скорость прохождения продольной и поперечной волны) и прочностными характеристиками. Акустические свойства горной породы необходимо принимать во внимание при интерпретации акустического каротажа скважин, который позволяет выявить распределение пород вдоль ствола скважины. Исходя из скоростей распространения ультразвуковых волн, можно вычислить динамический модуль упругости, который позволит оценить склонность скелета горной породы к уплотнению в результате действия эффективного напряжения. Поэтому определение акустических свойств горной породы необходимо при планировании разработки месторождения и ее осуществлении. Представлены результаты лабораторных исследований, направленных на установление зависимостей между прочностными и акустическими свойствами горной породы. В ходе эксперимента был также определен динамический модуль Юнга и выявлена его связь со скоростью распространения ультразвуковых волн. В результате лабораторных исследований получены эмпирические зависимости предела прочности при объемном сжатии (о,), динамическом модуле упругости (Е) и скорости прохождения продольных ( v\_) и поперечных волн ( v\_). Дана оценка полученных значений на всем диапазоне измерений.

Dmitriy G. Petrakov (Author ID in ORCID: http://orcid.org/0000-0002-0461-1621, Author ID in Scopus: 57015158900) – PhD in Engineering, Associate Professor at the Department of Development and Operation of Oil and Gas Fields (tel.: +007 921 788 19 62, e-mail: Petrakov\_DG@pers.spmi.ru). Grigorii M. Penkov (Author ID in ORCID: http://orcid.org/0000-0001-7291-0757, Author ID in Scopus: 57193449722) – PhD Student at the Department of Development and Operation of Oil and Gas Fields (tel.: +007 911 826 97 78, e-mail: penkovgrigoriy@gmail.com). The contact person for correspondence. Dmitry A. Solomoychenko (Author ID in Scopus: 57205736831) – PhD in Engineering, Senior Researcher at the Laboratory of Physical and Mechanical Properties and Fracture of Rocks (tel.: +007 953 149 08 16, e-mail: demo-@mail.ru).

Петраков Дмитрий Геннадьевич – кандидат технических наук, доцент кафедры разработки и эксплуатации нефтяных и газовых месторождений (тел.: +007 921 788 19 62, e-mail: Petrakov DG@pers.spmi.ru). Пеньков Григорий Михайлович – аспирант кафедры разработки и эксплуатации нефтяных и газовых месторождений (тел.: +007 911 826 97 78,

e-mail: penkovgrigoriy@gmail.com). Контактное лицо для переписки.

Соломойченко Дмитрий Анатольевич – кандидат технических наук, старший научный сотрудник лаборатории физико-механических свойств и разрушения горных пород (тел.: + 007 953 149 08 16, e-mail: demo-@mail.ru).

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## Introduction

The analysis of core material is a part of the mandatory procedure in the design of the hydrocarbon field development. As a result of core studies, various parameters are obtained which are necessary for building, for example, geological and hydrodynamic models. Such indicators can be:

- 1) filtration and capacity properties;
- 2) physical and mechanical properties, etc.

The listed properties play one of the leading roles when choosing a development system or planning activities aimed at enhancing reservoir oil recovery. Various authors [1–37] studied physical and mechanical properties of rock in carbonate and terrigenous deposits, including their strength characteristics.

The acoustic properties (propagation speed of longitudinal and transverse wave) of rock, same as those mentioned above, can be determined under laboratory conditions, since these indicators are necessary for the processing of formation logs and seismic data. Depending on these properties, the type of rocks that make up a productive horizon is determined. Also, based on these parameters, it is possible to calculate the dynamic elasticity (Young's modulus, Poisson's ratio) of rock. Knowing the dynamic elasticity parameters, it is possible to estimate how much the rock matrix is liable to compaction due to effective stress. A large number of works [38-42] are devoted to the determination of dynamic indicators of rock elasticity, as well as to the identification of relationship with the static data. Since the propagation speed of longitudinal and transverse waves depends on the type of rock and mode of occurrence, there is a need to determine these values for each hydrocarbon field separately. The determination of acoustic properties allows not only to identify dynamic elasticity indicators, but also to clarify some of the strength properties of rock. The laboratory studies were carried out in order to establish the relationship between the ultimate strength under volumetric compression, dynamic Young's modulus and acoustic properties of rock.

### **Experiment Procedure**

The experiment procedure can be divided into the following stages:

1. Preparation of samples for tests. The process of sample preparation includes: processing of end surfaces, measurment of the length, diameter and weight of the sample, sealing of the sample in a waterproof container, installation of sensors for measurment of longitudinal and transverse deformation, as well as for determination of acoustic properties of rock.

2. Performance of experiment:

a) the sample was put into the triaxial cell;

b) the cell was filled with working fluid. The temperature was set taking into account the formation conditions data (Table 1);

c) the overburden pressure and formation (pore) pressure was set step-by-step. The holding time at each stage was 5 minutes. At each stage, the side pressure increased by 3 MPa, and the pore pressure by 2 MPa;

d) the required values of formation and rock pressures (see Table 1) were established, the axial load was gradually increased until the sample destruction. Loading rate -1 MPa/s.

The measurement of the propagation speed of ultrasonic waves was carried out before the start of the test (the sample was not loaded), after reaching the formation conditions. The measurement of the longitudinal and transverse deformation value was carried out throughout the entire loading stage.

3. Processing of results.

3.1. Determination of static indicators. The ultimate strength under volumetric compression  $\sigma$  at the given rock and pore pressure for each sample was calculated by the formulas [43, 44]:

$$\sigma = \sigma_{\pi} + \sigma_{r} - \sigma_{\pi}, \qquad (1)$$

$$\sigma_{_{\mathcal{I}}} = \frac{P}{F},\tag{2}$$

where *P* – differential load applied to the ends of the sample, N; *F* – cross-sectional area of the sample, m<sup>2</sup>;  $\sigma_{\pi}$  – differential stresses, Pa;  $\sigma_{r}$  – rock pressure, Pa;  $\sigma_{\pi}$  – pore pressure, Pa.

Young's modulus and Poisson's ratio. Young's modulus (*E*) was determined on the linear section of the  $\sigma_{\pi} - \epsilon_{//}$  diagram as the ratio of the increment in differential stresses  $\Delta \sigma_{\pi}$  (to the increment of relative longitudinal deformations  $\Delta \epsilon_{//}$  [45, 46]:

$$E = \frac{\Delta \sigma_{\pi}}{\Delta \varepsilon_{//}} = \frac{\sigma_{\pi}^2 - \sigma_{\pi}^1}{\Delta \varepsilon_{//}^2 - \Delta \varepsilon_{//}^1} = \frac{op}{of}.$$
 (3)

3.2. Determination of dynamic parameters. The initial data for determination of the dynamic parameters were the differential load measured during the test, the time of longitudinal and transverse waves travel through the sample, and the sample density.

In accordance with the terms of reference and the test program, the dynamic indicators were determined by the following formulas [47, 48]:

- Young's modulus: 
$$E_d = \frac{\rho V_s^2 (3V_p^2 - 4V_s^2)}{V_p^2 - V_s^2};$$
 (4)

where  $V_{\rho}$ ,  $V_{\sigma}$ ,  $\rho$  – longitudinal wave speed, transverse wave speed and sample density, respectively;

- the speed of ultrasonic waves is determined by the formula [47, 49]:

$$V_i = \frac{L}{t_i},\tag{5}$$

where *L*- distance between the centers of transducers facility (sounding base), m;  $t_{\tau}$ - time of longitudinal (transverse) wave travel through the sample, s.

#### **Research Results**

Core samples of terrigenous sediments were taken from the X field to carry out the tests. 17 rock samples with the set formation conditions given in Table 1 were tested as part of the research.

Table 2 provides a geological description of these samples. After carrying out the experimental tests, the data were entered in the table (Table 3).

After determination of the dynamic characteristics of the samples, tests were carried out to determine the ultimate strength under volumetric compression. The results of the dependencies obtained following the laboratory studies are shown in Figure *a*, *b*.

In order to evaluate the accuracy of the identified dependencies, a check was carried out by determination of the values using these formulas and comparing with the values btained in the course of laboratory studies. The error in the calculated values is estimated by the distance from the diagonal line 1:1. The results of the check are presented in the figure: c, d.

Parameters of formation conditions set for rock samples testing

Item No.	Sample code	Formation	Test temperature, C	Pore pressure, MPa	Side pressure, MPa
1	2-BT-40	Lower Oligocene	140	21.3	83.1
2	3-BT-40	Lower Oligocene	140	21.3	83.1
3	6-BT-9	Upper Oligocene	136	35.1	85.0
4	7-BT-9	Upper Oligocene	136	35.1	84.9
5	8-BT-9	Upper Oligocene	136	35.1	82.9
6	11-BT-3	Lower Miocene	112	16.5	62.4
7	12-BT-116	Lower Miocene	108	22.6	66.4
8	13-BT-116	Lower Miocene	108	22.6	66.4
9	14-BT-4	Lower Miocene	108	22.6	62.6
10	15-BT-9	Upper Oligocene	136	35.1	82.6
11	18-DR-17	Lower Miocene	72	11.3	41.1
12	20-DR-29	Lower Miocene	78	12.0	33.6
13	21-DR-15	Lower Miocene	72	11.3	47.9
14	22-DR-15	Lower Miocene	72	11.3	47.9
15	24-DR-17	Lower Miocene	72	11.3	35.2
16	25-BT-9	Upper Oligocene	136	35.1	82.6
17	26-BT-9	Upper Oligocene	136	35.1	82.6

Table 2

Geological description of samples

Item	Sample	Formation	Interval.	Description
No.	code		Sampling depth	
1 2-BT	2-BT-40	Lower	Int. 3813.0-3822.0 m;	Brownish and gray, polymictic, arkosic, fine-to-medium grained sandstone with admixed large grains,
		Oligocene	depth 3820 m	evenly parallel medium-bedded
2 3-BT-40	Lower	Int. 3813.0-3822.0 m;	Brownish and gray, polymictic, arkosic, coarse-to-medium grained, massive sandstone with low-	
		Oligocene	depth 3813.4 m	carbonaceous sections
3 6-BT-9	6-BT-9	Upper	Int. 3798.0-3836.8 m;	Gray, polymictic, arkose, fine-grained, sorted, aleurolite sandstone
	Oligocene	depth 3826.3 m		
4	7-BT-9	Upper	Int. 3798.0-3836.8 m;	Gray and dark gray, polymictic, highly argillaceous siltstone (interlayers up to the transition to argillite),
<u> </u>		Oligocene	depth 3821.2 m	with parallel plane, cross and swaley bedding
5	8-BT-9	Upper	Int. 3720.6-3833.5 m;	Dark gray, coarse-grained, fine-areneceous, argillaceous, unevenly carbonaceous, highly micaceous,
0	0 21 9	Oligocene	depth 3732.2 m	finely parallel layered, dense siltstone
6	11-BT-3	Lower	Int. 2824.0-2841.8 m;	Brown sandstone as a result of oil saturation, polymictic, arkosic, medium-to-coarse grained, with
0 11	11-01-5	Miocene	depth 2827.0 m	admixed gravel, medium-graded, massive
7 12-BT-1	12-BT-116	5 Lower Miocene	Int. 3078.0-3092.5 m;	Light gray, quartz-feldspathic, fine-grained sorted massive sandstone
	12 01 110		depth 3079.5 m	Lon oray, quale recepting, inc brance, orice, incorre endotone
8 13-	13-BT-116	Lower	Int. 3078.0-3092.5 m;	Light gray, quartz-feldspathic, fine-grained sorted massive sandstone
	10 01 110	Miocene	depth 3078.6 m	ment gray, quar a reachanne, me granea, sorrea, massive sumatione
0 1	14-BT-4	Upper	Int. 2841.0-2844.0 m;	Brown sandstone as a result of oil saturation, polymictic, arkosic, medium-to-coarse grained, with
,	14-01-4	Oligocene	depth 2841.0 m	admixed gravel, medium-graded, massive
		Upper Oligocene	Int. 3720.0-3733.5 m; depth 3721.5 m	Interlensing of gray sandstone and dark gray siltstone. Polymictic, fine-grained sandstone with argillaceous-
10	15-BT-9			carbonaceous cement, highly micaceous (biotite, muscovite), dense, of medium strength. Argillaceous,
			deptil 5721.5 m	carbonaceous, highly micaceous, thin-layered siltstone
11	18-DR-17	Lower	Int. 2241.0-2249.0 m;	Variegated, cherry-brown sandstone with greenish-gray lenticular segments, quartz-arkose, fine-to-medium grained,
	10 Bit 17	Miocene	depth 2244.5 m	with uneven admixture of coarse sand and gravel grains
12	20-DB-20	Lower	Int. 2293.0-2302.0 m;	Brown, quartz-arkose, uneven-grained sandstone with admixed gravel material (grain size 1-8 mm),
12 20	20-Di(-2)	Miocene	depth 2296.6 m	turning into sand-gravel rock in some sections
13	21-DR-15	15 Lower	Int. 2170.0-2179.0 m;	Brownish and gray sandstone as a result of oil saturation, arkosic, with nonuniform structure, gradually
15	21-DIC15	Miocene	depth 2176.6 m	changing within the sample from coarse-to-medium grained to fine-to-medium grained
14	22-DR-15	Lower	Int. 2170.0-2179.0 m;	Greenish and gray, moderately sorted, sandy-argillaceous siltstone with an unclear layering pattern, rich
		Miocene	depth 2175.5 m	in mica (biotite, muscovite); dense
15	24 DP 14	Lower	Int. 1921.0-1929.0 m;	Variegated, cherry-brown sandstone with greenish and gray sections, quartz-arkose, fine-to-medium grained,
	27-01(-14	Miocene	depth 1921.5 m	with significant admixture of coarse grains and gravel
16	25-BT-9	Upper	Int. 3720.60-3733.50 m;	Interlensing of gray sandstone and dark gray siltstone. Fine-grained polymictic sandstone with carbonaceous-
10		Oligocene	depth 3723.5 m	argillaceous cement. Argillaceous, carbonaceous, highly micaceous, thin-layered siltstone
17	17 OC DT O	Upper	Int. 3720.60-3733.50 m;	Gray, polymictic, coarse-grained, fine-sandy, well-sorted siltstone with carbonaceous-argillaceous cement,
1/ 20	20-01-9	Oligocene	depth 3724.5 m	dense

Table 3

Results of determination of static parameters of rock samples and dynamic parameters after creation of formation conditions

			Static data			Dynamic data		
Item No.	Sample code	Formation	Ultimate strength, MPa	Young's modulus, 10⁴MPa	Density, kg/m³	Longitudinal wave speed, m/s	Transversal wave speed, m/s	Young's modulus, 10⁴MPa
1	2-BT-40	Lower Oligocene	124.1	1.54	2397	3359	2045	2.42
2	3-BT-40	Lower Oligocene	131.0	1.75	2346	3521	2142	2.60
3	6-BT-9	Upper Oligocene	115.8	1.64	2459	3587	2151	2.77
4	7-BT-9	Upper Oligocene	149.4	3.26	2497	4065	1921	2.50
5	8-BT-9	Upper Oligocene	209.7	1.84	2500	4679	2331	3.63
6	11-BT-3	Lower Miocene	107.6	1.50	2054	3450	1987	2.03
7	12-BT-116	Lower Miocene	111.4	1.95	2530	3635	1561	1.71
8	13-BT-116	Lower Miocene	121.3	2.04	2063	3800	1830	1.86
9	14-BT-4	Lower Miocene	161.5	2.12	2215	3359	1854	1.95
10	15-BT-9	Upper Oligocene	165.5	3.68	2440	3368	1964	2.34
11	18-DR-17	Lower Miocene	86.8	1.74	2190	2870	1470	1.25
12	20-DR-29	Lower Miocene	44.0	1.29	2091	2048	1165	0.72
13	21-DR-15	Lower Miocene	93.4	1.62	2207	3250	1530	1.40
14	22-DR-15	Lower Miocene	89.4	1.58	2340	3138	1450	1.34
15	24-DR-17	Lower Miocene	89.4	1.50	2341	2472	1434	1.20
16	25-BT-9	Upper Oligocene	152.0	3.45	2385	3678	1873	2.22
17	26-BT-9	Upper Oligocene	109.7	1.48	2315	3397	2074	2.40



Fig. Dependence on the propagation speed of longitudinal  $V_p$  and transverse  $V_s$  waves: a – ultimate strength under volumetric compression; b – dynamic elasticity modules; c – measured and calculated values of  $\sigma_c$ ; d – measured and calculated value of E

#### Conclusion

In the course of laboratory research, the following physical and mechanical parameters of rock were strength under determined: ultimate volumetric compression, static and dynamic elasticity modules, propagation speed of ultrasonic waves.

A relationship between the dynamic Young's modulus, the ultimate strength under volumetric compression, and the acoustic properties of rock was established. The obtained dependencies will make it possible to numerically evaluate strength and elasticity indicators when processing well logs or, for example, as a result of seismic data processing.

#### References

propagation speed of ultrasonic waves. **a result of selfsmit data processing. b data set house self-self-second processing second balance set house set house** 

# PERM JOURNAL OF PETROLEUM AND MINING ENGINEERING

37. Mubarak H. et al. Plasticity and Damage Analysis of Berea Sandstone via Cyclic Triaxial Loading Under High Confinement Pressure. 53rd US Rock Mechanics/Geomechanics Symposium. American Rock Mechanics Association, 2019, available at: https://onepetro.org/ARMAUSRMS/proceedings-abstract/ARMA19/AIRMA19/ARMA-2019-2082/125140 (accessed 02 December 2020).
38. Bakhorji A., Schmitt D.R. Laboratory measurements of static and dynamic bulk moduli in carbonate. 44th US Rock Mechanics Symposium and 5th US-Canada Rock Mechanics Symposium OnePetro, 2010. DOI: 10.1190/1.3255258
39. Yan F. et al. Comparison of dynamic and static bulk moduli of reservoir rocks. SEG Technical Program Expanded Abstracts 2017. Society of Exploration Geophysicists, 2017, pp. 3711-3715. DOI: 10.1190/j.segam2017-17664075.1
40. Siggins A.F., Dewhurst D.N. Saturation, pore pressure and effective stress from sandstone acoustic properties. *Geophysical Research Letters*, 2003, vol. 30, no. 2. DOI: 10.1029/2002GL016143
41. Olsen C., Christensen H.F., Fabricus IL. Static and dynamic Young's moduli of chalk from the North Sea. *Geophysical Research Letters*, 2003, vol. 30, no. 2. DOI: 10.10129/2002GL016143
42. Pen'kov G.M., Karmanskii D.A., Petrakov D.G. Issledovanie zavisimostei mezhdu fiziko-mekhanicheskimi svoistvami peschanika i skorost'iu prokhozhdeniia uprugikh voln [Studying the dependencies between the sandstone physical and mechanical properties and the elastic wave velocityl. *Vestnik Permskogo natsionalnogo issledovatel'skogo politekhnicheskogo universiteta. Geologia, neftegazovoe i gornoe delo,* 2020, vol. 20, no. 1. pp. 27-36. DOI: 10.15593/2224-9923/2020.1.3
43. Kovari K. et al. Suggested methods for determining the uniaxial compression: revised version. *Int J of Rock Mech & Mining Sci & Geomechanic As*, 1983, vol. 20, no. 6, pp. 285-290. DOI: 10.1016/0148-9062(39)90598-3
44. GOST 21153.8-88. Mountain rocks. Method for determining the uniaxial compression. *Intermation* 

#### Библиографический список

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